Name: $\qquad$

Section: $\qquad$

Last 4 digits of student ID \#: $\qquad$
This exam has twelve multiple choice questions (5 points each), five true/false questions (2 points each) and three free response questions (10 points each). Additional blank sheets are available if necessary for scratch work. No books or notes may be used. Turn off your cell phones and do not wear ear-plugs during the exam. You may use a calculator, but not one which has scientific or graphing capabilities.
On the multiple choice problems:

1. You must give your final answers in the multiple choice answer box on the front page of your exam. See the "EXAMPLE" row for a correct shading example.
2. Carefully check your answers. No credit will be given for answers other than those indicated on the multiple choice answer box.

## On the true/false choice problems:

1. You must give your final answers in the true/false choice answer box on the front page of your exam.
2. Carefully check your answers. No credit will be given for answers other than those indicated on the true/false choice answer box.

## On the free response problems:

1. Clearly indicate your answer and the reasoning used to arrive at that answer (unsupported answers may not receive credit),
2. Give exact answers, rather than decimal approximations to the answer (unless otherwise stated).
Each free response question is followed by space to write your answer. Please write your solutions neatly in the space below the question. You are not expected to write your solution next to the statement of the question.

Record the correct answer to the following problems on the front page of this exam.
Use the graph of $g$ below to answer questions 1-3.


1. If $t=2$, then $g(t+2.5)=$ $\qquad$
(a) 1
(b) 2
(c) 3
(d) 4.5
(e) 5
2. For what values of $x$ is $g(x)<0$ ?
(a) $[-3,0)$
(b) $[-2,0)$
(c) $(0,3]$
(d) $(0,4]$
(e) $(0,5]$
3. Determine the approximate interval where $g$ is decreasing.
(a) $[-2,3)$
(b) $(-2,4)$
(c) $[0,5]$
(d) $(3,5)$
(e) $(2,4)$
4. The rule of the function $g$ is given by the graph below. Determine the range.
(a) $[-3,3]$
(b) $[-2,3]$
(c) None of the other choices.
(d) $[-3,4]$
(e) $[-2,4]$

5. Jack and Jill are salespersons in the suit department of a clothing store. Jack is paid $\$ 200$ per week plus $\$ 5$ for each suit he sells, whereas Jill is paid $\$ 10$ for every suit she sells. If $f(x)$ represents Jack's weekly income and $g(x)$ represents Jill's weekly income from selling $x$ suits, then determine the rules of the functions $f$ and $g$.
(a) $f(x)=200 x+5 ; \quad g(x)=10$
(b) None of the other choices.
(c) $f(x)=200 x+5 ; \quad g(x)=10 x$
(d) $f(x)=5 x+200 ; \quad g(x)=10 x$
(e) $f(x)=5 x+200 ; \quad g(x)=10$
6. If $g(t)=t^{2}-t$ and $f(x)=1+x$, then compute $g(f(2)+3)$.
(a) 3
(b) 9
(c) 6
(d) 30
(e) 20
7. In a laboratory culture, the number $N(d)$ of bacteria (in thousands) at temperature $d$ degrees Celsius is given by the function $N(d)=-\frac{90}{d+1}+20$. The temperature $d(t)$ at time $t$ hours is given by the function $d(t)=2 t+4$. How many bacteria are in the culture after 4 hours?
$(\mathrm{a}) \approx 2,000$
(b) $\approx 8,000$
(c) $\approx 13,077$
(d) None of the other choices.
$(\mathrm{e}) \approx 16,400$
8. Which of the following graphs match the function $f(x)=(x+1)^{2}-1$ ?
(a)

(b)

(c)

(d)

(e) None of the other choices.
9. The table below shows the population $f(t)$ of rabbits on Christy's property $t$ years after she received 10 of them as a gift. Determine $3 \cdot f^{-1}(70)$.
(a) None of the other choices.
(b) 12
(c) 4
(d) 210
(e) 280

| $t$ | $f(t)$ |
| :--- | :---: |
| 0 | 10 |
| 1 | 23 |
| 2 | 48 |
| 3 | 64 |
| 4 | 70 |
| 5 | 71 |

10. If $f(x)=3 x-2$ and $g(x)=x^{2}$, then compute $(g \circ f)(3)$.
(a) 9
(b) 25
(c) 27
(d) 63
(e) None of the other choices.
11. Use the graph of $f(x)$ below to determine the graph of $-f(x)$.

(a)

(b)

(c)

(d)

(e) None of the other choices.
12. The function $f(x)=\sqrt{x+3}$ has an inverse. Which figure below is the graph of the inverse?
(a)

(b)

(c)

(d)

(e) None of the other choices.

For questions 13-17, determine whether each of the statements are either TRUE or FALSE.
13. A function may have different inputs with the same output.
14. The graph of a function has the property where no vertical line intersects the graph more than once.
15. The graph of $f(x)+3$ would be the graph of $f(x)$ shifted to the right 3 units.
16. Every function has an inverse.
17. If a function and its inverse are graphed on the same axes, then they are symmetric about the line $y=x$.
18. For the function $f(x)=x^{2}-x$, compute and simplify the difference quotient:

$$
\frac{f(x+h)-f(x)}{h}
$$

19. Sketch the graph of the following function, being sure to indicate which endpoints are included and which ones are excluded.

$$
f(x)= \begin{cases}x^{2}, & x \geq-1 \\ 2 x+3, & x<-1\end{cases}
$$


20. Use algebra to compute the inverse of the following one-to-one function:

$$
f(x)=\frac{3 x}{2-x}
$$

