MA 110 Alg and Trig for Calc Spring 2018 Exam 1 Tuesday, 6 February 2018

Name: $\qquad$

Section: $\qquad$

Last 4 digits of student ID \#: $\qquad$
This exam has twelve multiple choice questions (5 points each), five true/false questions (2 points each) and three free response questions (10 points each). Additional blank sheets are available if necessary for scratch work. No books or notes may be used. Turn off your cell phones and do not wear ear-plugs during the exam. You may use a calculator, but not one which has scientific or graphing capabilities.

## On the multiple choice problems:

1. You must give your final answers in the multiple choice answer box on the front page of your exam. See the "EXAMPLE" row for a correct shading example.
2. Carefully check your answers. No credit will be given for answers other than those indicated on the multiple choice answer box.

## On the true/false choice problems:

1. You must give your final answers in the true/false choice answer box on the front page of your exam.
2. Carefully check your answers. No credit will be given for answers other than those indicated on the true/false choice answer box.

## On the free response problems:

1. Clearly indicate your answer and the reasoning used to arrive at that answer (unsupported answers may not receive credit),
2. Give exact answers, rather than decimal approximations to the answer (unless otherwise stated).
Each free response question is followed by space to write your answer. Please write your solutions neatly in the space below the question. You are not expected to write your solution next to the statement of the question.

Multiple Choice Answers

| EXAMPLE | A | B | C | D | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Question |  |  |  |  |  |
| 1 | A | B | C | D | E |
| 2 | A | B | C | D | E |
| 3 | A | B | C | D | E |
| 4 | A | B | C | D | E |
| 5 | A | B | C | D | E |
| 6 | A | B | C | D | E |
| 7 | A | B | C | D | E |
| 8 | A | B | C | D | E |
| 9 | A | B | C | D | E |
| 10 | A | B | C | D | E |
| 11 | A | B | C | D | E |
| 12 | A | B | C | D | E |

True/False Choice Answers

| Question |  |  |
| :---: | :---: | :---: |
| 13 | T | F |
| 14 | T | F |
| 15 | T | F |
| 16 | T | F |
| 17 | T | F |

Exam Scores

| Exam Scores |  |  |
| :---: | ---: | ---: |
| Question | Score | Total |
| MC |  | 60 |
| TF |  | 10 |
| 18 |  | 10 |
| 19 |  | 10 |
| 20 |  | 10 |
| Total |  | 100 |

Record the correct answer to the following problems on the front page of this exam.
Use the graph of $f$ below to answer questions 1-3.


1. Determine the approximate interval where $f$ is increasing.
(a) $[-3,2]$
(b) $(0,3]$
(c) $(-3,3)$
(d) $(0,3)$
(e) $(3,5)$
2. For what values of $x$ is $f(x) \geq 0$ ?
(a) $[-3,0)$
(b) $[-3,0]$
(c) $(0,3)$
(d) $(0,5]$
(e) $[0,5]$
3. If $t=2$, then $f(t)-1.5=$
(a) 1
(b) 1.5
(c) 2
(d) 3.5
(e) 4
4. If $g(t)=t-t^{2}$ and $f(x)=2+x$, then compute $f(g(2)-1)$.
(a) -1
(b) 3
(c) None of the other choices
(d) -2
(e) 1
5. The rule of the function $f$ is given by the graph below. Determine the domain.
(a) $[-3,4]$
(b) $[-2,3]$
(c) $[-3,3) \cup(3,4]$
(d) None of the other choices.
(e) $[-3,3]$

6. Frank and Gracie are salespersons at an auto dealership. Frank is paid $\$ 175$ for each car he sells, whereas Gracie is paid $\$ 200$ per week, plus $\$ 50$ for every car she sells. If $f(x)$ represents Frank's weekly income and $g(x)$ represents Gracie's weekly income from selling $x$ suits, then determine the rules of the functions $f$ and $g$.
(a) $f(x)=175 ; \quad g(x)=200 x+50$
(b) $f(x)=175 x ; \quad g(x)=50 x+200$
(c) $f(x)=175 x ; \quad g(x)=200 x+50$
(d) $f(x)=175 ; \quad g(x)=50 x+200$
(e) None of the other choices
7. If $f(x)=3 x-2$ and $g(x)=x^{2}$, then compute $(f \circ g)(2)$.
(a) None of the other choices.
(b) 100
(c) 12
(d) 10
(e) 4
8. The function $f(x)=-\sqrt{x+3}$ has an inverse. Which figure below is the graph of the inverse?
(a)

(b)

(c)

(d)

(e) None of the other choices
9. Use the graph of $f(x)$ below to determine the graph of $f(x)-1$.
(a)

(b)

(c)

(d)

(e) None of the other choices
10. A pebble is dropped into a pond, making a circular wave. The radius of the wave, given by $r(t)=3 t$, increases 3 feet for every second that passes, where $t$ is in seconds and $r$ is in cm . The area of the wave is given by $A(r)=\pi r^{2}$. Compute the area of the wave after 3 seconds.
(a) $6 \pi \mathrm{~cm}^{2}$
(b) $9 \pi \mathrm{~cm}^{2}$
(c) $36 \pi \mathrm{~cm}^{2}$
(d) $81 \pi \mathrm{~cm}^{2}$
(e) None of the other choices.
11. The table below shows the population $f(t)$ of rabbits on Abigail's property $t$ years after she received 10 of them as a gift. Determine $4 \cdot f^{-1}(64)$.
(a) 3
(b) 12
(c) 192
(d) 256
(e) None of the other choices.

| $t$ | $f(t)$ |
| :---: | :---: |
| 0 | 10 |
| 1 | 23 |
| 2 | 48 |
| 3 | 64 |
| 4 | 70 |
| 5 | 71 |

12. Which of the following graphs match the function $f(x)=(x-1)^{2}-1$ ?
(a)

(b)

(c)

(d)

(e) None of the other choices

For questions 13-17, determine whether each of the statements are either TRUE or FALSE.
13. A function may have the same output with different inputs.
14. The graph of a one-to-one function has the property where no horizontal line intersects the graph more than once.
15. The graph of $f(x+5)$ would be the graph of $f(x)$ shifted right 5 units.
16. Not all functions have inverses.
17. When a function and its inverse are graphed on the same axes, they are symmetric about the $x$-axis.
18. For the function $f(x)=x^{2}+x-1$, compute and simplify the difference quotient:

$$
\frac{f(x+h)-f(x)}{h}
$$

19. Sketch the graph of the following function, being sure to indicate which endpoints are included and which ones are excluded.

$$
f(x)= \begin{cases}-2 x+5, & x \geq 3 \\ -x^{2}, & x<0\end{cases}
$$


20. Use algebra to compute the inverse of the following one-to-one function:

$$
f(x)=\frac{3-x}{2 x}
$$

