Answer all of the following questions. Additional sheets are available if necessary. No books or notes may be used. You may use a calculator. You may not use a calculator which has symbolic manipulation capabilities. When answering these questions, please be sure to 1) check answers when possible, 2) clearly indicate your answer and the reasoning used to arrive at that answer (unsupported answers may not receive credit).
Please lay out your solutions neatly in the space below the question. You are not expected to write each solution next to the statement of the question.
You are to answer two of the last three pages. Please indicate which page is not to be graded by drawing a line through its number on the table below. If you do not cross out one of the pages, we may assign credit for the two pages with the lowest scores.

Name $\qquad$
Section $\qquad$
Last four digits of student identification number $\qquad$

|  | Score | Possible |
| ---: | ---: | ---: |
| Page 1 |  | 14 |
| Page 2 |  | 14 |
| Page 3 |  | 14 |
| Page 4 |  | 14 |
| Page 5 | 14 |  |
| Page 6/Question 8 |  | 14 |
| Page 7/Question 9 |  | 14 |
| Page 8/Question 10 |  | 14 |
| Free | 2 | 2 |
|  |  | 100 |

1. Find the equation of a line passing through the point $(1,7)$ which is perpendicular to the line $6 x+3 y=9$. Express your answer in the form $y=m x+b$.

Answer: $\qquad$
2. Let $f$ and $g$ be functions which are defined by $f(x)=\sqrt{x-1}$ and $g(x)=1 / x$.
(a) Find the composition of $g$ and $f, g \circ f$.
(b) Give the domain of the composite function $g \circ f$.
(a) $g \circ f(x)=$
(b) The domain of $g \circ f$ is $\qquad$
3. At time $t=0$ seconds, a diver jumps from a diving board that is 10 meters above the water. The height of the diver measured in meters above the water at time $t$ seconds is given by the function $s(t)=-5 t^{2}+5 t+10$. Find the average velocity of the diver between $t=1$ second and $t=3 / 2$ seconds.

Average velocity = $\qquad$
4. Let $P_{1}, P_{2}, P_{3}, \ldots$ be a sequence of statements. Suppose it is known that:

- The statement $P_{3}$ is true.
- If $P_{n}$ is true, then $P_{n+2}$ is true.

Which of the statements $P_{2}, P_{3}, P_{4}, P_{5}, P_{6}, P_{7}$ and $P_{8}$ must be true? If none of these statements must be true, write "none" as the answer.
$\qquad$
5. Use our rules and theorems for limits to find the following limits. Be sure to give a clear statement of your reasoning.
(a) $\lim _{x \rightarrow 1} \frac{\sqrt{x}-1}{x-1}$
(b) $\lim _{x \rightarrow 2} \frac{x^{3}-27}{x+2}$
(c) $\lim _{x \rightarrow 7} \frac{x^{2}-49}{x-7}$
(a) $\lim _{x \rightarrow 1} \frac{\sqrt{x}-1}{x-1}=$ $\qquad$ (b) $\lim _{x \rightarrow 2} \frac{x^{3}-27}{x+2}=\square$,
(c) $\lim _{x \rightarrow 7} \frac{x^{2}-49}{x-7}=$
6. (a) Using the definition of the derivative, find the derivative of the function $f(x)=x^{2}+2$ at $x=1$.
(b) Find the equation of the tangent line to the graph of the function $f(x)=x^{2}+2$ at the point $(1,3)$. Put the equation of the tangent line in the form $y=m x+b$.
(a) $f^{\prime}(1)=$
(b)
7. Below, find the graph of a function $f$ on the interval $[0,4]$.
(a) Use the graph of $f$ to give the value of the limits.

$$
\begin{array}{ll}
\lim _{x \rightarrow 1^{-}} f(x)= & , \lim _{x \rightarrow 1^{+}} f(x)= \\
\lim _{x \rightarrow \frac{3}{2}^{-}} f(x)=
\end{array} \lim _{x \rightarrow \frac{3}{2}^{+}} f(x)=\square .
$$

(b) Is $f$ continuous at $x=1$ ? Explain.
(c) Is $f$ continuous at $x=3 / 2$ ? Explain.


Answer two of the following three questions. Indicate clearly which question is not to be graded by drawing a line through the question number in the table on the front of the exam.
8. (a) Give the definition of "continuity of a function $f$ at a number $a$ ". Use complete sentences.
(b) Let

$$
g(x)= \begin{cases}x^{2}, & x>3 \\ c x+2, & x \leq 3\end{cases}
$$

where $c$ is a number.
Find $\lim _{x \rightarrow 3^{+}} g(x)$ and $\lim _{x \rightarrow 3^{-}} g(x)$. The value for one of these limits will depend on the unknown number $c$.
(c) Find the value of $c$ so that the function $g$ is continuous at 3 . Explain why $g$ is continuous for this value of $c$.
9. (a) Give the definition of the derivative $f^{\prime}(x)$ of a function $f$ at a point $x$. Use complete sentences.
(b) Use the definition to find the derivative, $g^{\prime}(x)$, of the function $g(x)=\frac{1}{5 x+2}$.
(c) Give the domain of $g^{\prime}(x)$.
10. (a) State the intermediate value theorem. Use complete sentences.
(b) Find a closed interval $[a, b]$ so that the equation $x^{5}-2 x^{3}-4=x$ has a solution in the open interval $(a, b)$. Use the intermediate value to explain why you know there is a solution to the equation in the interval you found.

