MA 113 Calculus I Fall 2013 Exam 1 Tuesday, 24 September 2013

Name: _____

Section: _

Last 4 digits of student ID #:

This exam has ten multiple choice questions (five points each) and five free response questions (ten points each). Additional blank sheets are available if necessary for scratch work. No books or notes may be used. Turn off your cell phones and do not wear ear-plugs during the exam. You may use a calculator, but not one which has symbolic manipulation capabilities.

On the multiple choice problems:

- 1. You must give your *final answers* in the *multiple choice answer box* on the front page of your exam.
- 2. Carefully check your answers. No credit will be given for answers other than those indicated on the *multiple choice answer box*.

On the free response problems:

- 1. Clearly indicate your answer and the reasoning used to arrive at that answer (unsupported answers may not receive credit),
- 2. Give exact answers, rather than decimal approximations to the answer (unless otherwise stated).

Each free response question is followed by space to write your answer. Please write your solutions neatly in the space below the question. You are not expected to write your solution next to the statement of the question.

Multiple Choice Answers

Question					
1	A	В	С	D	Е
2	A	В	С	D	Е
3	A	В	С	D	Е
4	A	В	С	D	Е
5	A	В	С	D	Е
6	A	В	С	D	Е
7	A	В	С	D	Е
8	А	В	С	D	Е
9	А	В	С	D	Е
10	А	В	С	D	Е

Exam Scores

Question	Score	Total
MC		50
11		10
12		10
13		10
14		10
15		10
Total		100

- 1. Find the line that passes through the point (-2, 2) and is perpendicular to the line 2x + y = 1.
 - (A) y = -2x 2(B) $y = \frac{1}{2}x + 3$ (C) y = 2x + 6(D) $y = -\frac{1}{2}x + 1$ (E) y = -2x + 1

- 2. Suppose that f is a function of the form $f(x) = Ae^{kx}$, f(1) = 3 and f(3) = 12. Find A and k.
 - (A) A = 3/2, k = 2
 - (B) A = 3, k = 2
 - (C) A = 6, k = 2
 - (D) $A = 3/2, k = \ln(2)$
 - (E) $A = 3, k = \ln(2)$

3. Suppose that $\cos(\theta) = x$ and $\pi < \theta < 2\pi$. Find $\cos(-\theta)$ and $\sin(-\theta)$.

(A)
$$\cos(-\theta) = \sqrt{1 - x^2}$$
, $\sin(-\theta) = x$
(B) $\cos(-\theta) = -x$, $\sin(-\theta) = -\sqrt{1 - x^2}$
(C) $\cos(-\theta) = x$, $\sin(-\theta) = -\sqrt{1 - x^2}$
(D) $\cos(-\theta) = -x$, $\sin(-\theta) = \sqrt{1 - x^2}$
(E) $\cos(-\theta) = x$, $\sin(-\theta) = \sqrt{1 - x^2}$

4. If $\lim_{x\to 3} f(x) = 2$ and $\lim_{x\to 3} (f(x)g(x)) = -2$ find $\lim_{x\to 3} (2f(x) + g(x)).$ (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

5. Suppose that a function f is defined by

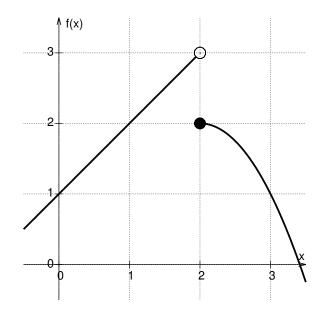
$$f(x) = \begin{cases} 2x - 1, & x < 2\\ c, & x = 2\\ x, & x > 2 \end{cases}$$

and we know that f is left-continuous at 2. Find c.

- (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) There is not enough information to answer this question.

- 6. Let the position of a particle be given by $p(t) = t^2$. Find the time *a* so that the average velocity of the particle for $2 \le t \le a$ is equal to 6.
 - (A) 2
 - (B) 3
 - (C) 4
 - (D) 5
 - (E) There is more than one correct answer.

- 7. Use the graph of f below to determine which of the following statements is true.
 - (A) f is continuous at x = 2
 - (B) $\lim_{x \to 2} f(x) = 2$
 - (C) $\lim_{x \to 2^+} f(x) = 3$
 - (D) $\lim_{x \to 2^{-}} f(x) = f(2)$
 - (E) $\lim_{x \to 2^{-}} f(x) = 3$



- 8. Let f and g be functions that are defined on the real line. Four of the statements are true for any functions f and g. One of the statements may fail for some choices of f and g. Which of the statements may be false?
 - (A) If f(1) = g(1), then $\lim_{x \to 1} f(x) = \lim_{x \to 1} g(x)$.
 - (B) If $\lim_{x \to 1} f(x) = \lim_{x \to 1} g(x)$, then $\lim_{x \to 1^+} f(x) = \lim_{x \to 1^+} g(x)$.
 - (C) If $\lim_{x \to 1} f(x) = 7$ and f is continuous at x = 1, then f(1) = 7.
 - (D) If $\lim_{x \to 1} f(x) = 2$ and $\lim_{x \to 1} g(x) = 3$, then $\lim_{x \to 1} (3f(x) 2g(x)) = 0$.
 - (E) If $\lim_{x \to 1^+} g(x) = \lim_{x \to 1^-} g(x) = 2$, then $\lim_{x \to 1} g(x) = 2$.
- 9. Suppose that $f(x) = (x 1)^2$, h(x) = 0, g is a function with domain $(-\infty, \infty)$, and $h(x) \le g(x) \le f(x)$ for all x. Then we can use the squeeze theorem to find
 - (A) $\lim_{x \to 0} g(x) = 0$
 - (B) $\lim_{x \to 0} g(x) = -1$
 - (C) $\lim_{x \to 0} g(x) = 1$
 - (D) $\lim_{x \to 1} g(x) = 0$
 - (E) $\lim_{x \to 1} g(x) = 1$

10. Find the value of the limit $\lim_{x \to 0} \frac{\tan(2x)}{x}$.

- (A) -2
- (B) -1
- (C) 0
- (D) 1
- (E) 2

- 11. A rectangle has perimeter of 30 meters.
 - (a) Make a sketch of the rectangle and label the sides in your sketch. Write a function A that gives the area of the rectangle as a function of the length of one of the sides.
 - (b) Give the domain of the function A. The sides of a rectangle cannot be of negative length, but we allow the cases where one of the sides is of length 0.

12. Let $f(x) = \frac{x+2}{x-3}$. Find the inverse function f^{-1} and the domain and range of f^{-1} .

13. Let $f(x) = \frac{1}{2x - 1}$.

- (a) Find the slope of the line that passes through the points (1, f(1)) and (1 + h, f(1 + h)). Simplify your answer.
- (b) Take the limit as h tends to zero of the expression found in part a). Use the limit laws to justify your evaluation of the limit.
- (c) Give the geometric interpretation of your answer to part (b).

14. For each limit below, find the limit if it exists or explain why it does not exist. Carefully justify your answers.

(a)
$$\lim_{x \to 1} \frac{e^x(x-1)}{x^2-1}$$
.

(b)
$$\lim_{x \to 1} \frac{e^x(x+1)}{x^2 - 1}$$
.

- 15. (a) State the Intermediate Value Theorem.
 - (b) Use the Intermediate Value Theorem to find an interval that contains a solution of the equation

$$x^3 + x + 1 = -3$$