MA 113 Calculus I Spring 2017 Exam 1 Tuesday, February 7, 2017

| Name: | | | |
|------------|--|------|--|
| | | | |
| Section: _ | | | |

Last 4 digits of student ID #:

This exam has five true/false questions (two points each), ten multiple choice questions (five points each) and four free response questions (ten points each). Additional blank sheets are available if necessary for scratch work. No books or notes may be used. Turn off your cell phones and do not wear ear-plugs during the exam. You may use a calculator, but not one which has symbolic manipulation capabilities.

On the true/false and multiple choice problems:

- 1. You must give your final answers in the front page answer box on the front page of your exam.
- 2. Carefully check your answers. No credit will be given for answers other than those indicated on the *front page answer box*.

On the free response problems:

- 1. Clearly indicate your answer and the reasoning used to arrive at that answer (unsupported answers may not receive credit),
- 2. Give exact answers, rather than decimal approximations to the answer (unless otherwise stated).

Each free response question is followed by space to write your answer. Please write your solutions neatly in the space below the question. You are not expected to write your solution next to the statement of the question.

| True/False | | |
|------------|---|-----|
| 1 | | F |
| 2 | Т | |
| 3 | Ţ | F |
| 4 | Т | 'n |
| 5 | Т | 170 |

| <u> </u> | | | (200 C) | | |
|-----------------|-----|---|--------------|---|---|
| Multiple Choice | | | | | |
| 6 | A | В | С | D | E |
| 7 | A | В | C | D | E |
| 8 | A | В | \mathbf{C} | Ď | Е |
| 9 | A * | В | C | D | E |
| 10 | A | В | С | D | Ė |
| 11 | A | В | \mathbf{C} | D | E |
| 12 | A | В | | D | Ē |
| 13 | A | В | C | D | |
| 14 | A | | Ċ | D | Е |
| 15 | A | В | Ö | D | E |

Overall Exam Scores

| Question | Score | Total |
|----------|-------|-------|
| TF | | 10 |
| MC | | 50 |
| 16 | | 10 |
| 17 | | 10 |
| 18 | | 10 |
| 19 | | 10 |
| Total | | 100 |

Free Response Questions: Show your work!

(a) Find all solutions to the equation $2 \ln(x) - \ln(1+x) = \ln(1)$.

$$\ln(x^2) - \ln(1+x) = \ln(1)$$

$$\Rightarrow$$
 $\left(N\left(\frac{X^{2}}{1+X}\right)=N(1)\right)$

Solves are
$$1\pm\sqrt{5}$$
, but $1\pm\sqrt{5}$ is not in denominable.

(b) Suppose that $f(x) = Ae^{kx}$. If f(0) = 20 and f(3) = 17, then find A and k. You do not need to simplify your answer.

Free Response Questions: Show your work!

17. Evaluate the following limits, or explain why the limit does not exist. Show all your work.

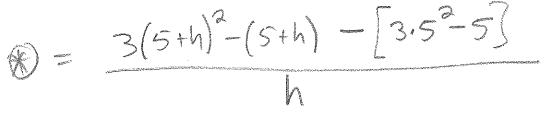
(a)
$$\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$$
 $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$ $\lim_{x \to \infty} \frac{3x^4 - x^2 + x - \pi}{7x^4 - 3x^3 + 1}$

(b)
$$\lim_{x\to\infty} \left[\sqrt{4x^2 + 1} - 2x \right] = \lim_{x\to\infty} \left(\sqrt{4x^2 + 1} - 2x \right) \cdot \left(\sqrt{4x^2 + 1} + 2x \right)$$

$$= \lim_{x\to\infty} \frac{4x^2 + 1 - 4x^2}{\sqrt{4x^2 + 1} + 2x} = \lim_{x\to\infty} \frac{4x^2 + 1 - 2x}{\sqrt{4x^2 + 1} + 2x} = 0.$$

Free Response Questions: Show your work!

- 18. Suppose a particle has position $f(x) = 3x^2 x$ meters at time x seconds.
 - (a) Find a formula for the average velocity of the particle over the time interval [5, 5+h]. You do not need to simplify your answer.



(b) Estimate the instantaneous velocity of the particle at time 5 seconds using the following three values for h: -0.1, 0.1, 0.01

Plug these into @ .

(c) Take the limit as h tends to zero of the expression found in part (a) to find the instantaneous velocity of the particle at 5 seconds. Use the limit laws to justify your evaluation of the limit.

$$\lim \Re = \lim_{h \to 0} \frac{3(25 + 10h + h^2) - (5 + h) - 3.25 + 5}{h}$$

$$= \lim_{h \to 0} \frac{3(25 + 10h + h^2) - (5 + h) - 3.25 + 5}{h} = 29.7$$

$$= \lim_{h \to 0} \frac{30h + 3h^2 - h}{h} = \lim_{h \to 0} 29 + 3h = 29.7$$

19. (a) State the intermediate value theorem.

See textbk

(b) If $g(x) = x^2 + 5^x - 3$, use the intermediate value theorem to show that there is a number a such that g(a) = 10.

$$g(0) = 0^{2} + 5^{0} - 3 = -2$$
,
 $g(2) = 2^{2} + 5^{2} - 3 = 29 - 3 = 26$,

Since g(x) is a polynomial, it is cts. Since $g(0) = -2 \times 10 \times g(2) = 26$, by IVT $g(0) = -2 \times 10 \times g(2) = 10$ on [0,2]. There is a solu g(a) = 10 on [0,2].