

Name: \_\_\_\_\_ Section: \_\_\_\_\_

Answer all questions and show your work. Unsupported answers may receive *no credit*. You may not use a calculator on this quiz. Allow 15 minutes for the quiz.

1. Find the following integrals

(a) (3 points)  $\int x \sin(2x) dx$

**Solution:** Set  $u = x$ ,  $dv = \sin(2x) dx$  so  $du = 1 dx$  and  $v = -\frac{1}{2} \cos(2x)$ . Then

$$\begin{aligned} \int x \sin(2x) dx &= -\frac{x}{2} \cos(2x) + \frac{1}{2} \int \cos(2x) 1 dx \\ &= -\frac{x}{2} \cos(2x) + \frac{1}{4} \sin(2x) + C \end{aligned}$$

(1 point) for correct  $u$ ,  $dv$ , (1 point) for correct integration by parts, (1 point) for answer, including  $+C$ .

(b) (4 points)  $\int_0^2 x e^{x^2+1} dx$

**Solution:** Use the substitution  $u = x^2 + 1$ . Thus  $\frac{1}{2} du = x dx$  and when  $x = 0$ ,  $u = 1$  and when  $x = 2$ ,  $u = 5$  to obtain

$$\begin{aligned} \int_0^2 x e^{x^2+1} dx &= \frac{1}{2} \int_1^5 e^u du \\ &= e^u \Big|_{u=1}^5 \\ &= e^5 - e. \end{aligned}$$

Defining  $u$  and  $du$  (1 point). Writing integral in terms of  $u$  (1 point). Changing limits (1 point). Answer (1 point).

Do not accept numerical answers without supporting work.

Allow other solution methods. If a student finds the anti-derivative in terms and  $x$  and then evaluates at 0 and 2, give two points for correct answer.

(c) (3 points)  $\int x^3 \ln(x) dx$ .

HINT: Use integration by parts with  $dv = x^3 dx$  and  $u = \ln(x)$ .

**Solution:** Following the hint, we have  $u = \ln(x)$ ,  $du = \frac{1}{x} dx$ ,  $v = \frac{1}{4} x^4$  and  $dv = x^3 dx$ .

Using integration by parts, we have

$$\begin{aligned}\int x^3 \ln(x) dx &= \frac{1}{4}x^4 \ln(x) - \frac{1}{4} \int x^4 \frac{1}{x} dx \\ &= \frac{1}{4}x^4 \ln(x) - \frac{1}{4} \int x^3 dx \\ &= \frac{1}{4}x^4 \ln(x) - \frac{1}{16}x^4 + C.\end{aligned}$$

Listing  $u$ ,  $du$ ,  $v$ , and  $dv$  (1 point). Integrating by parts correctly (1 point).

Answer (1 point).

Deduct one point if  $+C$  is missing, but only deduct once for this mistake.