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# Math 213 - Labelling Space

Peter A. Perry

University of Kentucky

August 26, 2019

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- Access your WebWork account only through Canvas!
- Homework A1 on Sections 12.1-12.2 is due Friday August 30
- Applications for an alternate Exam 1 are due **no later than September 4**

Review your schedule and apply for all alternate exams at once by using the Google Form linked from Canvas or the course home page.

# Calc I-II Calc III 2D to 3D Spheres Review 000000 000 000 0 0 0

# Unit I: Geometry and Motion in Space

- 12.1 Lecture 1: Three-Dimensional Coordinate Systems
- 12.2 Lecture 2: Vectors in the Plane and in Space
- 12.3 Lecture 3: The Dot Product
- 12.4 Lecture 4: The Cross Product
- 12.5 Lecture 5: Equations of Lines and Planes, I
- 12.5 Lecture 6: Equations of Lines and Planes, II
- 12.6 Lecture 7: Surfaces in Space
- 13.1 Lecture 8: Vector Functions and Space Curves
- 13.2 Lecture 9 Derivatives and Integrals of Vector Functions Lecture 10: Exam I Review



# Learning Goals

- Review basics of Calculus I-II
- Preview Calculus III
- Introduce 3D coordinate systems
- Introduce the distance formula in 3D
- Find equations of spheres

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## What Happened in Calculus I-II?

The derivative of a function

$$f'(x_0) = \lim_{h \to 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

computes:

- The slope of the tangent line to the graph of y = f(x) at  $x = x_0$
- The instantaneous rate of change of a function f at  $x = x_0$

Using the derivative, you can find: intervals of increase and decrease, local extrema, and global extrema. It will be important to remember the *differential* of f,

$$df(x) = f'(x) \, dx$$

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# What Happened in Calculus I-II?

The *integral* of a function *f*:

$$\int_{a}^{b} f(x) \, dx$$

computes:

- The net area under the graph of y = f(x) between *a* and *b*
- The net change in a quantity *F* with rate of change *f*(*x*) = *F*'(*x*) between *x* = *a* and *x* = *b*

The integral is a limit of *Riemann sums*. Any geometric quantity (area, arc length, volume) or physical quantity (displacement given velocity, velocity given acceleration) that can be computed as a limit of Riemann sums can be computed as an integral

#### The Fundamental Theorem of Calculus

**Fundamental Theorem, Part I** If f is continuous on [a, b] and F is any antiderivative of f, then

$$\int_{a}^{b} f(x) \, dx = F(b) - F(a)$$

**Fundamental Theorem, Part II** If *f* is a continuous function on [*a*, *b*] then

$$\frac{d}{dx}\left(\int_{a}^{x}f(t)\,dt\right) = f(x)$$

In other words,

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$$\int df = d\left(\int f\right) = f$$

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# What will happen in Calculus III?

In Calculus III we'll take these concepts of Calculus into higher dimensions

- We'll consider *vector functions*  $\mathbf{v}(t) = (x(t), y(t))$  and  $\mathbf{w}(t) = (x(t), y(t), z(t))$  which describe motion in the plane and in space
- We'll consider *functions of several variables* f(x, y) and g(x, y, z) which describe altitude, temperature distributions, densities, etc.
- We'll learn about *transformations* (*x*(*u*, *v*), *y*(*u*, *v*)) that generalize polar coordinates and describe regions
- We'll study *parameterized* surfaces (*x*(*u*, *v*), *y*(*u*, *v*), *z*(*u*, *v*))
- We'll consider *vector fields* which describe the velocity of a fluid, the force of gravity, the action of electric and magnetic fields, and more!

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We will move into three-dimensional space



This choice of x-, y-, z-axes forms a right-handed coordinate system

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We will move into three-dimensional space



This choice of *x*-, *y*-, *z*-axes forms a *right-handed coordinate system* 

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We will move into three-dimensional space



To locate a point *P* with respect to a chosen origin *O*, we specify the *x*, *y* and *z* displacements from *O*. For example, the point P = (1, 2, 3) is obtained by moving:

• 1 unit in the *x* direction

This choice of *x*-, *y*-, *z*-axes forms a *right-handed coordinate system* 



We will move into three-dimensional space



To locate a point *P* with respect to a chosen origin *O*, we specify the *x*, *y* and *z* displacements from *O*. For example, the point P = (1, 2, 3) is obtained by moving:

- 1 unit in the *x* direction
- 2 units in the y direction

This choice of *x*-, *y*-, *z*-axes forms a *right-handed coordinate system* 

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# Calc I-II Calc I-II 2D to 3D Spheres Review 00000 000 00 00 00 00

# What Will Happen Today?

We will move into three-dimensional space



To locate a point *P* with respect to a chosen origin *O*, we specify the *x*, *y* and *z* displacements from *O*. For example, the point P = (1, 2, 3) is obtained by moving:

- 1 unit in the *x* direction
- 2 units in the *y* direction
- 3 units in the *z* direction

This choice of *x*-, *y*-, *z*-axes forms a *right-handed coordinate system* 

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$$P = (2, 1, -1)$$

is obtained by moving:



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$$P = (2, 1, -1)$$

is obtained by moving:

• 2 units in the *x* direction

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The point

$$P = (2, 1, -1)$$

is obtained by moving:

- 2 units in the *x* direction
- 1 unit in the *y* direction

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The point

$$P = (2, 1, -1)$$

is obtained by moving:

- 2 units in the *x* direction
- 1 unit in the *y* direction
- -1 units in the *z* direction

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# The Distance Formula in $\mathbb{R}^2$

Recall the distance between two points in the *xy* plane:





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 Calc I-II
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 Spheres
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The Distance Formula in  $\mathbb{R}^2$ 

Recall the distance between two points in the *xy* plane:



# The Distance Formula in $\mathbb{R}^2$

Recall the distance between two points in the *xy* plane:

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Add an "extra" point *Q* below  $P_2$ By the Pythagorean Theorem,  $|P_1P_2|^2 = |P_1Q_1|^2 + |QP_2|^2$ 

 $\mathbf{so}$ 

$$P_1 P_2 | = \sqrt{|P_1 Q_1|^2 + |Q P_2|^2}$$
$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

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### The Distance Formula in $\mathbb{R}^3$





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# The Distance Formula in $\mathbb{R}^3$



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# The Distance Formula in $\mathbb{R}^3$



Add an "extra" point Q

• By the Pythagorean Theorem,

$$|P_1P_2|^2 = |P_1Q|^2 + |QP_2|^2$$

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# The Distance Formula in $\mathbb{R}^3$



Add an "extra" point Q

• By the Pythagorean Theorem,

$$|P_1P_2|^2 = |P_1Q|^2 + |QP_2|^2$$

• By the two-dimensional distance formula

$$|P_1Q|^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2$$

while

$$|QP_2|^2 = (z_2 - z_1)^2$$

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# The Distance Formula in $\mathbb{R}^3$



Add an "extra" point Q

• By the Pythagorean Theorem,

$$|P_1P_2|^2 = |P_1Q|^2 + |QP_2|^2$$

• By the two-dimensional distance formula

$$|P_1Q|^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2$$

while

$$|QP_2|^2 = (z_2 - z_1)^2$$

$$P_1P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

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 Calc III
 2D to 3D
 Spheres
 Review

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### Two and Three Dimensions



Find the set of all points (x, y) that satisfy the equation x = 2



 Calc I-II
 Calc III
 2D to 3D
 Spheres
 Review

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### Two and Three Dimensions



Find the set of all points (x, y) that satisfy the equation x = 2

*Answer:* A vertical line through x = 2





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Find the set of all points (x, y) that satisfy the

Answer: A vertical line through x = 2

Find the set of all points (x, y, z) that obey the

Answer: A vertical plane through y = 2

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 Spheres
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Two and Three Dimensions



Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$



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Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0, 0)



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Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0,0)

Find the set of all points (x, y, z) that satisfy the equation

$$x^2 + y^2 = 1$$

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Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0,0)

Find the set of all points (x, y, z) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A cylinder of radius 1 centered at (0,0,0) whose axis of symmetry is the *z*-axis

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Two and Three Dimensions



Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$



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Two and Three Dimensions



Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0,0)



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Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0,0)

Find the set of all points (x, y, z) that satisfy the equation

$$x^2 + y^2 + z^2 = 1$$

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Find the set of all points (x, y) that satisfy the equation

$$x^2 + y^2 = 1$$

Answer: A circle of radius 1 centered at (0,0)

Find the set of all points (x, y, z) that satisfy the equation

$$x^2 + y^2 + z^2 = 1$$

Answer: A sphere of radius 1 centered at (0,0,0).

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Find the set of points (x, y) that satisfy the *inequality* 

$$1 < x^2 + y^2 < 4$$

Answer: The annulus centered at (0,0) and bounded by circles of radii 1 and 2



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Find the set of points (x, y) that satisfy the *inequality* 

$$1 < x^2 + y^2 < 4$$

Answer: The annulus centered at (0,0) and bounded by circles of radii 1 and 2

Find the set of all points (x, y, z) that satisfy the *inequality* 

$$1 < x^2 + y^2 + z^2 < 4$$

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Find the set of points (x, y) that satisfy the *inequality* 

$$1 < x^2 + y^2 < 4$$

Answer: The annulus centered at (0,0) and bounded by circles of radii 1 and 2

Find the set of all points (x, y, z) that satisfy the *inequality* 

$$1 < x^2 + y^2 + z^2 < 4$$

Answer: The spherical shell centered at (0,0) with inner radius 1 and outer radius 2

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### The Two Most Important Formulas in this Lecture

**Distance Formula in Three Dimensions** The distance  $|P_1P_2|$  between  $P_1(x_1, y_1, z_1)$  and  $P_2(x_2, y_2, z_2)$  is

$$P_1P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

**Equation of a Sphere** The equation of a sphere with center  $(h, k, \ell)$  and radius *r* is

$$(x-h)^{2} + (y-k)^{2} + (z-\ell)^{2} = r^{2}$$

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# Some Examples

Find the equation of a sphere with center at (-9, 4, 8) and radius 3.



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### Some Examples

Find the equation of a sphere with center at (-9, 4, 8) and radius 3.

Answer: Using the distance formula on  $P_1(-9,4,8)$  and  $P_2(x,y,z)$  we see that

$$(x+9)^2 + (y-4)^2 + (z-8)^2 = 3^2$$

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### Some Examples, Part II

Find the equation of a sphere if one of its diameters has endpoints  $P_1(9, 1, -8)$  and  $P_2(11, 5, -2)$ .

Here we'll need to use the given information to find the radius and the center.



# Some Examples, Part II

Find the equation of a sphere if one of its diameters has endpoints  $P_1(9, 1, -8)$  and  $P_2(11, 5, -2)$ .

Here we'll need to use the given information to find the radius and the center.

Find the radius by finding the distance between the endpoints of the diameter:



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# Some Examples, Part II

Find the equation of a sphere if one of its diameters has endpoints  $P_1(9, 1, -8)$  and  $P_2(11, 5, -2)$ .

Here we'll need to use the given information to find the radius and the center.

Find the radius by finding the distance between the endpoints of the diameter:

$$|P_1P_2| = \sqrt{(11-9)^2 + (5-1)^2 + (-2-(-8))^2} = \sqrt{56}$$
 so  $r^2 = d^2/4 = 14$  (why?)

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### Some Examples, Part II

Find the equation of a sphere if one of its diameters has endpoints  $P_1(9, 1, -8)$  and  $P_2(11, 5, -2)$ .

Here we'll need to use the given information to find the radius and the center.

Find the radius by finding the distance between the endpoints of the diameter:

$$|P_1P_2| = \sqrt{(11-9)^2 + (5-1)^2 + (-2-(-8))^2} = \sqrt{56}$$
  
 $r^2 = d^2/4 = 14$  (why?)

Find the center  $P(h, k, \ell)$  by finding the midpoint between  $P_1$  and  $P_2$ :

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### Some Examples, Part II

Find the equation of a sphere if one of its diameters has endpoints  $P_1(9, 1, -8)$  and  $P_2(11, 5, -2)$ .

Here we'll need to use the given information to find the radius and the center.

Find the radius by finding the distance between the endpoints of the diameter:

$$|P_1P_2| = \sqrt{(11-9)^2 + (5-1)^2 + (-2-(-8))^2} = \sqrt{56}$$
 so  $r^2 = d^2/4 = 14$  (why?)

Find the center  $P(h, k, \ell)$  by finding the midpoint between  $P_1$  and  $P_2$ :

$$(h,k,\ell) = \left(\frac{9+11}{2}, \frac{1+5}{2}, \frac{-8-2}{2}\right) = (10,3,-5)$$

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You should now be able to find the equation of the sphere.



### Lecture Review

- We introduced 'right-handed' coordinate systems in three-dimensional (*xyz*) space
- We derived the *distance formula* for the distance between two points in three-dimensional space

$$|P_1P_2| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

- We worked out and graphed equations for planes, cylinders, and spheres in three-dimensional space
- I reminded you to access WebWork only through Canvas!

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### Homework

Be sure to prepare for recitation tomorrow:

- Study section 12.1, pp. 792–796
- Download recitation worksheet and review Worksheet 1 on section 12.1
- Create your Webwork account by *logging in through Canvas*
- Begin Webwork Assignment A1 Remember to access WebWork *only through Canvas!*

For Wednesday, read and study section 12.2, pp. 798-804.

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